## Measurement of the Proton Spin Structure Function $g_{1}\left(x, Q^{2}\right)$ for $Q^{2}$ from 0.15 to 1.6 $\mathrm{GeV}^{2}$ with CLAS

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(Dated: February 4, 2008)


#### Abstract

Double-polarization asymmetries for inclusive $e p$ scattering were measured at Jefferson Lab using 2.6 and 4.3 GeV longitudinally polarized electrons incident on a longitudinally polarized $\mathrm{NH}_{3}$ target in the CLAS detector. The polarized structure function $g_{1}\left(x, Q^{2}\right)$ was extracted throughout the nucleon resonance region and into the deep inelastic regime, for $Q^{2}=0.15-1.64 \mathrm{GeV}^{2}$. The contributions to the first moment $\Gamma_{1}\left(Q^{2}\right)=\int g_{1}\left(x, Q^{2}\right) d x$ were determined up to $Q^{2}=1.2 \mathrm{GeV}^{2}$. Using a parametrization for $g_{1}$ in the unmeasured low $x$ regions, the complete first moment was estimated over this $Q^{2}$ region. A rapid change in $\Gamma_{1}$ is observed for $Q^{2}<1 \mathrm{GeV}^{2}$, with a sign change near $Q^{2}=0.3 \mathrm{GeV}^{2}$, indicating dominant contributions from the resonance region. At $Q^{2}=1.2$ $\mathrm{GeV}^{2}$ our data are below the pQCD evolved scaling value.


PACS numbers: $13.40 . \mathrm{Gp}, 13.60 . \mathrm{Hb}, 14.20 . \mathrm{Dh}$

Electron scattering has played a long and distinguished role in the study of nucleon structure. Inclusive deep inelastic scattering (DIS) studies 1] revealed the parton constituents (quarks and gluons) of the nucleon. At low values of the four momentum transfer $Q^{2}$ the nucleon structure functions depend on both $Q^{2}$ and on the energy transfer $\nu=E_{0}-E^{\prime}$, where $E_{0}$ and $E^{\prime}$ are the initial and final electron energies. In the asymptotic limit, $Q^{2} \rightarrow$ $\infty$, the scattering is described by perturbative Quantum Chromodynamics (pQCD) as the absorption of a virtual photon on a single free quark. In this limit the structure functions depend only on the Bjorken scaling variable, $x=Q^{2} / 2 M \nu$, where $M$ is the nucleon mass.

When both the incident electron and the target nucleon are polarized (double-polarization) the scattering cross section depends on two additional functions of $Q^{2}$ and $\nu, g_{1}$ and $g_{2}$. In the framework of pQCD these also depend only on $x$ as $Q^{2} \rightarrow \infty$. In this limit $g_{1}(x)$ has a simple interpretation as the sum over the $x$-dependent polarizations of the various quark flavors. A doublepolarization experiment at CERN showed that in the framework of asymptotic QCD only a fraction of the nucleon spin could be attributed to the intrinsic spin of the quarks. These measurements were confirmed by subsequent experiments at CERN, SLAC, and DESY, (see the reviews [2, 3] and references therein). Corrections (higher-twist terms) for finite $Q^{2}$ result in excellent fits to the extensive data set for $Q^{2}$ down to the order of 2 $\mathrm{GeV}^{2}$. It is generally accepted that the intrinsic spin of
the quarks accounts for about $25 \%$ of the nucleon spin, so that other degrees of freedom, such as gluons and quark orbital angular momentum, must account for the rest.

Until recently, only a few double-polarization experiments were carried out with energies below 25 GeV , an important example being the ground-breaking experiment at SLAC [4] in the late 1970's. More recently, the spin structure function $g_{1}$ and its first moment $\Gamma_{1}\left(Q^{2}\right)=\int g_{1}\left(x, Q^{2}\right) d x$ have become a focus at lower $Q^{2}$ and in the resonance region in experiments at SLAC [5], Hermes [6, 7], and JLab [8, 9] to obtain a better understanding of QCD in the confinement regime and to study the phenomenon of duality between the resonance region and the deep inelastic region. The rapidly changing helicity structure of some resonances as a function of $\mathrm{Q}^{2}$ is expected to have a strong influence on $g_{1}$. Double-polarization measurements at lower energies can therefore indicate where pQCD breaks down and determine where multi-parton processes and coherent effects due to nucleon resonance transitions are important.

For inclusive scattering of electrons and protons polarized along the axis of the electron beam, the doublepolarization asymmetry is given by:

$$
\begin{equation*}
A_{e x p}=\frac{\sigma^{\uparrow \downarrow}-\sigma^{\uparrow \uparrow}}{\sigma^{\uparrow \downarrow}+\sigma^{\uparrow \uparrow}}=\sqrt{1-\epsilon^{2}} \cos \theta_{\gamma}\left[\frac{A_{1}+\eta A_{2}}{1+\epsilon R}\right] \tag{1}
\end{equation*}
$$

where $\sigma^{\uparrow \uparrow}$ and $\sigma^{\uparrow \downarrow}$ are the cross sections for the electron and proton spins parallel and anti-parallel, respectively.

The factor $\epsilon=\left[1+2\left(1+\nu^{2} / Q^{2}\right) \tan ^{2}(\theta / 2)\right]^{-1}$ is the virtual photon polarization for electron scattering angle $\theta$. The parameter $R=\sigma_{L} / \sigma_{T}$ is the ratio of the absorption cross sections for longitudinal and transverse virtual photons. The kinematical factor $\eta=\epsilon \sqrt{Q^{2}} /\left(E_{0}-\epsilon E^{\prime}\right)$. The angle between the virtual photon, $\gamma^{*}$, and the beam direction is given by $\theta_{\gamma}$.

The photon asymmetries $A_{1}$ and $A_{2}$ can be written in terms of the virtual photon absorption cross sections as:

$$
\begin{equation*}
A_{1}\left(x, Q^{2}\right)=\frac{\sigma_{T}^{1 / 2}-\sigma_{T}^{3 / 2}}{2 \sigma_{T}}, \quad A_{2}\left(x, Q^{2}\right)=\frac{\sigma_{L T}}{\sigma_{T}} \tag{2}
\end{equation*}
$$

in which $\sigma_{T}^{1 / 2}$ and $\sigma_{T}^{3 / 2}$ are transverse cross sections and $\sigma_{T}$ is half their sum. The superscripts denote the helicity of the $\gamma^{*} p$ system. The cross section $\sigma_{L T}$ arises from longitudinal-transverse interference. In the nucleon resonance region the relative contributions of helicity $1 / 2$ and $3 / 2$ vary from one resonance to another and depend strongly on $Q^{2}$. The spin structure function $g_{1}$ is linearly related to $A_{1}$ and $A_{2}$ by:

$$
\begin{equation*}
g_{1}\left(x, Q^{2}\right)=\frac{\nu^{2}}{Q^{2}+\nu^{2}}\left(A_{1}+\sqrt{\frac{Q^{2}}{\nu^{2}}} A_{2}\right) F_{1}\left(x, Q^{2}\right) \tag{3}
\end{equation*}
$$

where $F_{1}$ is a structure function appearing in the unpolarized electron scattering cross section.

If the contribution from elastic scattering $(x=1)$ is excluded, $\Gamma_{1}$ vanishes at $Q^{2}=0$, where, in addition, its slope is constrained to be negative by the Gerasimov-Drell-Hearn (GDH) sum rule 10, 11] for absorption of real photons. The validity of the GDH sum rule has been experimentally tested to better than $10 \%$ by experiments at Mainz [12] and at ELSA [13]. On the other hand, $\Gamma_{1}$ is known to be positive at high $Q^{2}$ [2, 3]. Therefore, the constraints near $Q^{2}=0$ and at high $Q^{2}$ imply that $\Gamma_{1}$ must change sign at some low $Q^{2}$, where it is expected to be dominated by the nucleon resonances [14, 15].

At low $Q^{2}$, meson-baryon dynamics have been treated in chiral perturbation theory by Ji and Osborne [16] and by Bernard, Hemmert, and Meissner 17] to evolve $\Gamma_{1}$ to non-zero values of $Q^{2}$. Badelek, Kwieciǹski, and Ziaja 18] have used the generalized vector dominance model and GDH to make predictions for $g_{1}(x)$ at low $\mathrm{Q}^{2}$. At high $Q^{2}$ the asymptotic value of $\Gamma_{1}$ has been evolved down to $Q^{2}=1 \mathrm{GeV}^{2}$ by using pQCD and the Operator Product Expansion [19]. Phenomenological approaches, either with explicit inclusion of resonance parameters 20, 21] or with general parametrizations of structure functions 22], have been used to cover the entire $Q^{2}$ range.

The present measurements were carried out with 2.6 and 4.3 GeV longitudinally polarized electrons incident on a longitudinally polarized target located at the center of the CLAS detector [23]. A toroidal magnetic
field, symmetric about the beam axis, is generated by six super-conducting coils. The coils separate the detector into six independent spectrometers that use wire drift chambers for track reconstruction, scintillation counters for time-of-flight measurements, threshold gas Cerenkov counters, and lead-scintillator electromagnetic calorimeters. Electrons can be detected and identified for momenta down to $0.35 \mathrm{GeV} / \mathrm{c}$ and for polar angles from about $8^{\circ}$ to $50^{\circ}$. The polarization of the beam, which was measured frequently with a Møller polarimeter, was typically $70 \%$. The beam helicity was flipped at a rate of 1 Hz in a pseudo-random sequence to minimize systematic effects.

A microwave pumped solid nuclear target 24] using the method of Dynamic Nuclear Polarization [25] was built for the CLAS. Its design is similar to those employed in experiments at SLAC [5]. Horizontal cylinders, $\sim 1 \mathrm{~cm}$ long, were packed with ammonia pellets (either ${ }^{15} \mathrm{NH}_{3}$ or ${ }^{15} \mathrm{ND}_{3}$ ). The cylinders were mounted with their axes along the beam line on a movable ladder, along with an empty cup and a 2.2 mm thick carbon disk. The target cell was immersed in a liquid He bath at $\mathrm{T}=1.2 \mathrm{~K}$. A pair of super-conducting Helmholtz coils coaxial with the beam generated a uniform 5 T magnetic field in the target volume. A maximum proton polarization of $70 \%$ was obtained. During beam irradiation the proton polarization typically dropped gradually to $40 \%$, at which point the target material was removed and replaced in order to restore the original polarization.

Charged particles were identified from the measured momentum and time-of-flight. The Cerenkov counters and calorimeters were used to reduce the $\pi^{-}$contamination in the electron sample to less than $1 \%$. The scattered electrons were binned according to $Q^{2}$ and the invariant mass $W=\left(M^{2}+2 M \nu-Q^{2}\right)^{1 / 2}$ of the recoiling hadronic system. For each bin the polarization asymmetry defined in eqn. 1 is:

$$
\begin{equation*}
A_{\exp }=C_{N} C_{p s} \frac{1}{P_{e} P_{t}}\left(\frac{N^{\downarrow \uparrow}-N^{\uparrow \uparrow}}{N^{\downarrow \uparrow}+N^{\uparrow \uparrow}-N_{b k g}}\right)+A_{R C} \tag{4}
\end{equation*}
$$

in which $P_{e}$ and $P_{t}$ are the averaged polarizations of the electrons and protons, respectively; $N^{\uparrow \uparrow}$ and $N^{\downarrow \uparrow}$ are the number of observed electrons normalized to the total incident beam flux for parallel and anti-parallel beam and target spins; and $N_{b k g}$ is the number of electrons scattered from unpolarized material, which consists of He , ${ }^{15} \mathrm{~N}$, target windows, and foils used to isolate vacuum regions. The factor $C_{N}=0.98$ corrects for the contribution of polarized protons in the ${ }^{15} \mathrm{~N}$ [5]. The "pair-symmetric" correction $C_{p s}$ and the radiative correction term $A_{R C}$ are discussed below.

The background $N_{b k g}$ accounts for approximately $85 \%$ of the detected electrons, and it was determined from an analysis of runs using the carbon target. Comparisons of the carbon and ammonia scattering rates for $W>$ 1.4 GeV were used to extract the mass thickness of the
ammonia. The known densities and thicknesses of the materials in the beam-line, along with a parametrization of the ratio of the free proton and neutron cross sections to account for the unpaired proton in ${ }^{15} \mathrm{~N}$, were used to calculate $N_{b k g}$ from the carbon target data.

Eq. 4 does not include corrections for detector acceptance or efficiency since, except for possible changes in the detector between ammonia and carbon runs, these cancel in the ratio. Less than $5 \%$ of the data showed short-term localized changes in the detector. The affected regions were removed from the analysis.

The polarization product $P_{e} P_{t}$ for each set of runs was extracted directly by comparing the measured asymmetry for elastic scattering to the known elastic ep asymmetry. Two independent procedures were followed. In the first method, the background-subtracted asymmetry was obtained in several $Q^{2}$ bins, checked for consistency, and averaged. The second method exploited a limited kinematical range in which both the scattered electron and recoil proton could be detected. The strict correlation in angle and momentum for elastic ep scattering distinguishes it from inelastic $e p$ scattering and from quasielastic scattering in nitrogen without subtracting a background spectrum. The two methods were consistent with each other. A typical value was $P_{e} P_{t}=(36 \pm 1) \%$.


FIG. 1: The photon asymmetry $A_{1}+\eta A_{2}$ vs. the invariant hadronic mass $W(\mathrm{GeV})$ for the proton in two $Q^{2}$ bins. The lower $Q^{2}$ data were obtained with a beam energy of 2.6 GeV and the higher with 4.3 GeV . The dashed curves show our model estimates of $\eta A_{2}$. The error bars denote statistical uncertainties and the shaded bands near the bottom of the plot indicate the magnitude of the systematic uncertainties (1 $\sigma$ ).

A "pair-symmetric" correction $C_{p s}$ was made for the contribution of $\pi^{0} \rightarrow e^{+} e^{-} \gamma$ to the inclusive electron sample. It was determined by measuring the $e^{+}$rate with opposite torus current. Since the correction rises very sharply at high $W$ (low scattered electron energy), we analyzed data only in the kinematic region where the pair-symmetric background was less than $10 \%$ of the total electron rate.

Radiative corrections were applied to the experimen-
tal asymmetries using the code RCSLACPOL [5], developed at SLAC and based on the approach of Kuchto and Shumeiko [26] for the internal corrections, and by Tsai 27] for external corrections. We used parametrizations of the world data on unpolarized and polarized structure functions (including our own preliminary asymmetry data) and elastic form factors as input for the radiative correction code. Details of this model will be given in a longer paper.

The model used for radiative corrections was also used to calculate values for $A_{1}, A_{2}, g_{1}, g_{2}, F_{1}, F_{2}$, and $R$ over the measured region of $Q^{2}$ and $x$. Using the calculated value of $R$, Eq. was used to obtain $A_{1}+\eta A_{2}$ from the corrected experimental asymmetry defined by Eq. 4 The results for two representative $Q^{2}$ bins are shown in Fig. 1 The model values of $\eta A_{2}$ were generally small, as can be seen from the dashed curves in Fig. 1 These calculated values were used to extract $A_{1}$ from the measured $A_{\text {exp }}$. Finally, we used the model for $F_{1}$ and $A_{2}$, along with Eq. 3 to extract $g_{1}$, which is dominated by $A_{1}$. The results for $g_{1}$ for the proton for five $Q^{2}$ bins are shown in Fig. 2 The solid curve shows $g_{1}$ calculated from the data parametrization used in RCSLACPOL.


FIG. 2: The polarized structure function $g_{1}(x)$ vs. $x$ for the proton for five $Q^{2}$ bins. The solid lines show the parametrization described in the text. The error bars denote statistical uncertainties and the shaded area at the bottom of each plot indicates the magnitude of the systematic uncertainties ( $1 \sigma$ ).

We can integrate $g_{1}\left(x, Q^{2}\right)$ from the lowest measured value of $x$ (with a cut-off ranging from $W=2$ to 2.6 GeV ) up to $x=1$ at each $Q^{2}$ to obtain the contribution of our data to the integral $\Gamma_{1}$ (the contribution of elastic scat-
tering is excluded). The results are shown as the closed circles in Fig. 3 The full value of the integral was estimated by using the parametrization for $g_{1}$ to estimate the contribution from $x=10^{-5}$ up to the threshold of our measurements. These extended integrations are shown as open circles. The plot is cut off at $Q^{2}=1.2 \mathrm{GeV}^{2}$ since at higher values more than half the integral is due to the unmeasured region of $x$. The slope at $Q^{2}=0$


FIG. 3: The first moment $\Gamma_{1}$ vs. $Q^{2}$ for the proton. The closed circles are obtained by integrating over our measurements of $g_{1}$. The open circles are obtained by using the inclusive scattering model to extend the integral down to $x=10^{-5}$. The error bars indicate statistical uncertainties. The dark shaded region at the bottom shows the estimated systematic uncertainties $(1 \sigma)$ for the measured points. The line above the shaded region indicates the systematic uncertainty for the open circles. Measurements from SLAC [5] are shown as shaded squares with the double error bar indicating statistical uncertainty and (statistical + systematic) uncertainties. See the text for an explanation of the curves.
required by the GDH sum rule is indicated by a straight line. Calculations using the light baryon ChPT formulation of Bernard et al. 17] are indicated by a shaded band at $Q^{2}<0.2 \mathrm{GeV}^{2}$ with boundaries that reflect uncertainties in resonance parameters. The pQCD evolution of the deep inelastic scattering measurements to $\mathcal{O}\left(\alpha_{s}^{3}\right)$ [19] is shown as a line at high $Q^{2}$. The calculations of Soffer and Teryaev [22] and Burkert and Ioffe [20] in the intermediate region are also shown. A linear fit to the five points from $Q^{2}=0.20$ to $0.47 \mathrm{GeV}^{2}$ yields a zero crossing for $\Gamma_{1}$ at $Q^{2}=0.29 \pm 0.03 \mathrm{GeV}^{2}$, where the error includes only the statistical uncertainty and the estimated uncertainty in the DIS contribution added in quadrature. The zero crossing indicates the transition to a distance scale where
non-partonic contributions such as resonance excitations are dominant. Our results for $\Gamma_{1}\left(Q^{2}\right)$ lie well below the predictions from the pQCD evolution from DIS. They are in better agreement with the model calculations of Ref. 20] that include s-channel baryon resonance excitations explicitly. Thus, we think that it is likely that the lack of explicit inclusion of the resonance contributions in the pQCD evolution gives rise to the discrepancy.

The estimated systematic uncertainties $(1 \sigma)$ are indicated by the shaded band at the bottom of each plot in the figures. The systematic uncertainty is dominated by the parametrizations of $A_{2}, F_{1}$ and $R$, which constitute $75 \%$ of the total uncertainty at low $Q^{2}$ and $50 \%$ at high $Q^{2}$. The uncertainty is estimated by using alternative parametrizations, as well as by setting $R$ and $\mathrm{A}_{2}$ to extreme values. The radiative corrections, which also incorporate these models, constitute $20 \%$ of the total systematic uncertainty at low $Q^{2}$ and $5 \%$ at high $Q^{2}$. The remaining uncertainty arises largely from livetime calculations and the removal of the nuclear contributions from the ammonia spectra. The systematic uncertainty of the DIS extrapolation for Fig. [3 was estimated by using three different parametrizations for $g_{1}$ in the low $x$ region, Simula 21], and the previously mentioned model fitted to world data before 1999 and 2000, respectively.

In summary, our measured asymmetries for inclusive scattering of 2.6 and 4.3 GeV polarized electrons on polarized protons have been used to extract the structure function $g_{1}\left(x, Q^{2}\right)$ for $Q^{2}$ from 0.15 to $1.64 \mathrm{GeV}^{2}$. The first moment $\Gamma_{1}$ depends strongly on $Q^{2}$, with its sign changing near $Q^{2}=0.3 \mathrm{GeV}^{2}$.

We would like to acknowledge the outstanding efforts of the staff of the Accelerator, the Target Group, and the Physics Divisions at JLab who made this experiment possible. This work was supported in part by the U.S. Department of Energy, the U.S. National Science Foundation, the Istituto Nazionale di Fisica Nucleare, the French Centre National de la Recherche Scientifique, the French Commissariat à l'Energie Atomique, and the Korean Science and Engineering Foundation. The Southeastern Universities Research Association (SURA) operates the Thomas Jefferson National Accelerator Facility for the United States Department of Energy under contract DE-AC05-84ER40150.

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